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# Decadal and quadratic variations of Earth's oblateness and polar ice mass balance from 1979 to 2010

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# SUMMARY

Gravity variations associated with Earth's oblateness  $(J_2)$  have been observed by satellite laser ranging (SLR) since 1976. The  $J_2$  time-series has been used to measure and help understand many geophysical processes within the Earth system ranging from the mantle to the atmosphere. While post glacial rebound and the Earth climate system are believed to be the primary driving forces of long-term and seasonal  $J_2$  variations, the physical cause of decadal and longer timescale  $J_2$  variations has remained uncertain, although recent evidence indicates that polar ice mass changes are important. In this study, we estimate a variety of climate contributions to  $J_2$  over the period 1979–2010, and find that ice mass variations in Greenland and Antarctica are the dominant cause of observed decadal and longer  $J_2$  variations. Residual variations at periods near 10–11 years may reflect limitations of numerical climate models in estimating mass change variability at long periods, but are also suggestive of potential contribution related to variable solar activity.

Key words: Satellite geodesy; Time variable gravity; Global change from geodesy.

### **1 INTRODUCTION**

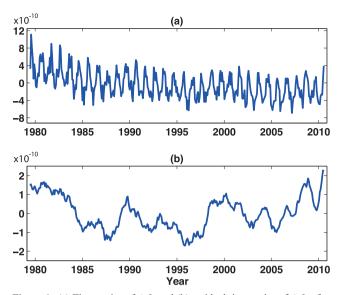
One of the most prominent features in Earth's shape is the equatorial bulge, mainly a consequence of Earth's rotation. This oblateness of Earth produces the largest departure of Earth's gravity from that of a spherically symmetric body, and is measured by the  $J_2$  (degree 2, order 0) coefficient of gravity in a spherical harmonic representation.  $J_2$  changes over a broad spectrum of timescales, ranging from tidal to seasonal to the age of the Earth. The range of associated physical causes implies that  $J_2$  variations are a useful global measure of large-scale mass redistribution within the Earth system.

 $J_2$  variations have been measured by satellite laser ranging (SLR) since 1976, starting with the launch of LAGEOS. The dominant elements of the  $J_2$  time-series are a negative trend with superimposed seasonal variability. The negative trend indicates that Earth is becoming less oblate, mostly due to Post Glacial Rebound (PGR; Yoder *et al.* 1983) and polar ice mass loss (Nerem & Wahr 2011). Seasonal variations reflect redistribution of air and water mass between tropical and extra-tropical regions (Gutierrez & Wilson 1987). As longer  $J_2$  time-series became available, interannual and decadal signals were revealed. These timescales are likely to be climate-related, possibly tied to glacier melting, variations such as the El Niño-Southern Oscillation (ENSO) and the Pacific Decadal Oscillation (PDO), or to the 18.6-yr ocean tide (Cox & Chao 2002; Dickey *et al.* 2002; Cheng & Tapley 2004).

Recently, Cheng et al. (2013) examined  $J_2$  variations from 1976 to 2011 and suggested that accelerating ice mass loss from glaciers and ice sheets is probably one of the causes that may explain longterm variations. Nerem & Wahr (2011) showed that  $J_2$  variations can be largely explained by polar ice mass changes from 2002 to 2010 based on GRACE observations over Greenland and Antarctica. A remaining question is accounting for  $J_2$  variations in the pre-GRACE era. A main problem has been limitations of both observations and models of climate-related mass redistribution. This is particularly true for polar region where long-term ice mass changes have been poorly observed over a large part of the nearly four-decade span of the  $J_2$  time-series prior to GRACE. Here we investigate a variety of sources, especially those related to Greenland and Antarctic ice mass changes for the period 1979–2010.  $J_2$  comparison between observations and models should be useful to validate the estimate of polar ice mass changes as well as to understand earth oblateness variations for the last four decades.

 $J_2$  variations ( $\Delta J_2$ ) are estimated from multiple satellite SLR observations (Cheng *et al.* 2013), and are available from the GRACE Tellus website (http://grace.jpl.nasa.gov/data/j2).  $\Delta J_2$  is given at 30-d intervals, and is resampled here to monthly values (centered in the middle of the month) to compare with monthly climate model series (Fig. 1a). Since causes of the linear trend and seasonal variations are relatively well known (Yoder *et al.* 1983; Gutierrez & Wilson 1987; Nerem & Wahr 2011), our examination focuses on interannual and longer variations by removing the linear trend and seasonal terms

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**Figure 1.** (a) Time-series of  $\Delta J_2$  and (b) residual time-series of  $\Delta J_2$  after removing linear trends and seasonal cycles by least squares.

from  $\Delta J_2$ . In addition, we apply an 11-month moving average to suppress high frequencies in the residual  $\Delta J_2$ . The resulting timeseries of  $\Delta J_2$  is dominated by interannual, decadal and quadratic variations (Fig. 1b). In the next section, we develop estimates of various climate-related contributions in order to explain variations in Fig. 1(b).

# 2 CLIMATE CONTRIBUTIONS TO $\Delta J_2$

Change of surface mass density,  $\Delta \sigma(\theta, \phi)$ , driven by geophysical or climate variations alter  $J_2$ , and can be calculated by integration over Earth's surface (Chao *et al.* 1987):

$$\Delta J_2 = -\frac{1+k_2}{5} \frac{R_e^2}{M_e} \int \Delta \sigma(\theta, \phi) P_2(\cos \theta) \,\mathrm{d}S \tag{1}$$

in which  $k_2 = -0.303$  is the Earth's degree 2 load Love number (Han & Wahr 1995),  $R_e$  and  $M_e$  are the mean radius and mass of the Earth, respectively.  $P_2(\cos\theta)$  is the Legendre polynomial (spherical harmonic), and  $\theta$  and  $\phi$  are latitude and longitude, respectively. To calculate  $\Delta J_2$ , we use  $\Delta \sigma(\theta, \phi)$  from multiple climate models and observations.

We estimate continental water contributions to  $\Delta J_2$  using the Global Land Data Assimilation System Version 2 (GLDAS-2) (Rodell et al. 2004), available from 1948 to 2010. GLDAS-2 is forced by a climatologically consistent data set whereas forcing in the earlier version (GLDAS-1) created spurious trends, making it unsuitable for long-term terrestrial water estimates (Rui & Beaudoing 2013). In addition, contemporary hydrology models are probably inadequate to understand long-term terrestrial water variations since they are designed to maintain long-term water balance. As a result, Cheng et al. (2013) excluded continental water variations in their  $\Delta J_2$  study. Here we use only soil moisture contribution to  $\Delta J_2$ . The ERA-Interim surface pressure field (Simmons *et al.* 2007) is used for terrestrial atmospheric mass variations including Greenland and Antarctica. For ocean mass variations (bottom pressure), we combine ERA-Interim surface pressure with an inverted barometer assumption and ocean mass redistribution from GECCO (German partner of the Estimating the Circulation and Climate of the Ocean; Stammer et al. 2004). GECCO is forced by NCEP fields available from 1952 to 2011. GECCO is used in place of ECCO

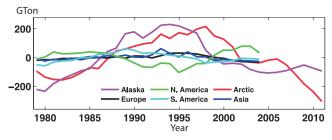


Figure 2. Glacier mass balance on the continents including Alaska. Linear trends are removed.

which depends upon assimilated satellite altimeteric observations starting in 1992. Because GECCO does not conserve mass, mass conservation is imposed here by removing changes in mean ocean mass every month. Seasonal cycles and linear trends are removed from soil moisture, surface pressure and ocean bottom pressure time-series.

Mountain glacier contributions are estimated using glacier mass balance data (Dyurgerov 2002) from the National Snow & Ice Data Center (NSIDC) (http://nsidc.org/data/G10002). Annual mountain glacier mass balance rates are available from 1961 to 2003. Fig. 2 shows the detrended cumulative continental glacier mass balance rate from 1979 to 2003 including Alaska. The time-series for Alaska and the Arctic is extended to 2010 using GRACE Release 5 (RL05) solutions provided by the Center for Space Research, University of Texas at Austin. Leakage bias due to the limited degree and order of GRACE spherical harmonics and spatial filtering is corrected using unconstrained global forward modelling (Chen et al. 2014). Glacier effects from other regions might also be estimated using GRACE, but the task is more difficult due to spatial leakage from adjacent hydrologic signals. There is some indication that mountain glacier storage in other areas is more stable (Jacob et al. 2012). In addition, glacier contributions from mid-latitudes, where the degree 2 order 0 spherical harmonic is small, would have a diminished effect on  $\Delta J_2$ . Thus we include only Alaska and Arctic glacier effects on  $\Delta J_2$ .  $\Delta J_2$  comparisons between Alaska/Arctic glaciers and other area are shown below.

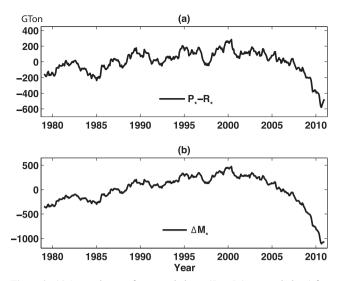
Polar ice mass variations from 1979 to 2010 are estimated from climate models and satellite observations. These changes can be separated into effects of surface mass balance (*SMB*) and ice discharge (D),

$$\Delta M_{T_0}^T(\theta, \phi) = \int_{T_0}^T SMB(\theta, \phi) \, \mathrm{d}t - \int_{T_0}^T D(\theta, \phi) \, \mathrm{d}t$$
$$= \int_{T_0}^T \left( P(\theta, \phi) - R(\theta, \phi) \right) \, \mathrm{d}t - \int_{T_0}^T D(\theta, \phi) \, \mathrm{d}t \qquad (2)$$

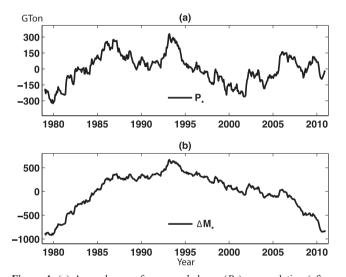
*SMB* depends on the difference between precipitation (*P*) and runoff (*R*). We ignore minor components of ice mass balance such as sublimation (Lenaerts *et al.* 2012) and basal melting of grounded ice. We remove linear trends and seasonal terms from each component of eq. (2). The time integrated residuals (denoted by  $_*$ ) are related by

$$\Delta M_* = P_* - R_* - D_*, \tag{3}$$

where  $\Delta M_*$ ,  $P_*$ ,  $R_*$  and  $D_*$  are residual ice mass changes and accumulations of precipitation, meltwater runoff and ice discharge, respectively. We use a regional climate model, RACMO2 (van Angelen *et al.* 2012) for  $P_*-R_*$  in Greenland. In Antarctica,  $R_*$ is nearly zero because surface melting and rainfall are minor and refrozen in snowpack (van Wessem *et al.* 2014). Therefore, for *SMB* 



**Figure 3.** (a) Anomalous surface mass balance  $(P_* - R_*)$  accumulation (after removing seasonal cycles and linear trends) and anomalous ice mass balance  $(\Delta M_*)$  including surface mass balance and ice discharge in Greenland.



**Figure 4.** (a) Anomalous surface mass balance  $(P_*)$  accumulation (after removing seasonal cycles and linear trends) and ice mass balance  $(\Delta M_*)$  including surface mass balance and ice discharge in Antarctica.

in Antarctica, we only use ERA-Interim precipitation results (Simmons *et al.* 2007). Medley *et al.* (2013) found that reanalysis precipitation variations agree better with in-situ data than the regional climate model estimates in Antarctica. In addition, ERA-Interim is superior among contemporary global reanalysis in estimating precipitation change at high southern latitudes (Bromwich *et al.* 2011). Figs 3(a) and 4(a) show Greenland  $P_*-R_*$  and Antarctic  $P_*$ , respectively.

There are limited observations and models of  $D_*$  which is a measure of departures of ice discharge from a constant rate. These would reflect changing ice dynamics, including acceleration of discharge over time. Long-term (1958–2007) annual ice discharge in Greenland was reported in Rignot *et al.* (2008b): East and west Greenland experienced ice discharge increases during the last two decades while ice discharge variation in the east was stable from 2005 to 2007. Similar ice discharge variations were examined for 2000–2012 (Enderlin *et al.* 2014): In the west, ice discharge has

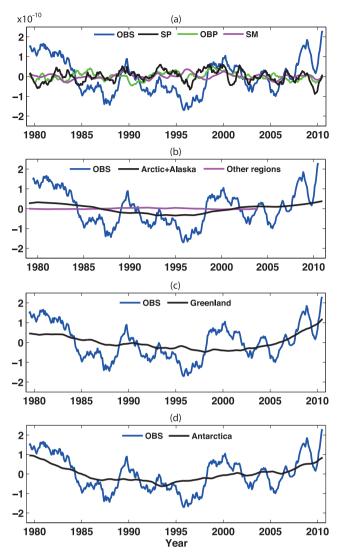
increased about 3 GTon yr<sup>-1</sup> since 2000, and in the southeast, it increased from 2000 to 2004 and has been stable since 2005. For  $D_*$ from 1979 to 2010, we combine ice discharge estimates from both studies of Rignot *et al.* (2008b) and Enderlin *et al.* (2014). Fig. 3(b) shows  $\Delta M_*$  (=  $P_* - R_* - D_*$ ) in Greenland. Evident ice mass loss acceleration occurred during the last decade resulting mainly from similar acceleration in  $P_* - R_*$  (Sasgen *et al.* 2012; Seo *et al.* 2015a).

Several studies also showed that ice discharge has increased in the Antarctic Peninsula (AP) and Amundsen Sea Sector (AS; Rignot et al. 2008a). Mouginot et al. (2014) estimated the annual ice discharge based on Landsat and satellite radar interferometry from 1974 to 2013. Most recently, Seo et al. (2015b) also quantified  $D_*$ in AS and AP from 2003 to 2013 based on GRACE observation accounting for SMB variations and atmospheric pressure errors. The two  $D_*$  estimates in AS are remarkably similar to each other during the common period (Seo *et al.* 2015b), and thus we use  $D_*$  in AS from the estimates by Mouginot et al. (2014). Unlike in AS, detailed ice discharge variations in AP during the last three decades have not been reported yet. However, Seo et al. (2015b) showed that the acceleration rate in AP  $D_*$  is about 5.0 GTon yr<sup>-2</sup>, corresponding to coefficient  $a_1$  in a least square fit of the form  $a_0 + a_1 \frac{1}{2} (t - t_0)^2$ to  $D_*$ , where  $t_0$  is the middle of the given period. Rignot *et al.* (2008a) also showed that the AP ice discharge increased from 107 to 136 GTton  $yr^{-1}$  during 10 yr (1996–2006), equivalent to the acceleration rate of about 5.8 GTon yr<sup>-2</sup>, which is very close to the GRACE-based study. Therefore, for  $D_*$  in AP, we use the acceleration (quadratic) component, 5.0 GTon  $yr^{-2}$ , for the entire period (1979-2010) under the reasonable assumption that Antarctic ice dynamic variations have long (decadal) timescales. Fig. 4(b) shows  $\Delta M_* = P_* - D_*$  in Antarctica.

A final step in the calculation is to enforce water mass conservation for the globe by computing the terrestrial mass anomaly from all effects (soil moisture, mountain glaciers and ice sheets). Ocean mass is adjusted by this amount, by adding or subtracting a uniform layer of water. Although the spatial pattern of the adjusted ocean mass is not uniform due to the nature of self-gravitation of fluid on Earth's envelope (Farrell & Clark 1976), this procedure considers the first order water mass redistribution between land and oceans.

# 3 $\Delta J_2$ COMPARISON BETWEEN MODEL AND OBSERVATION

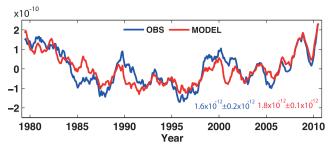
Fig. 5(a) shows observed (blue from Fig. 1b) and estimated (black, green and magenta)  $\Delta J_2$  representing effects of surface pressure, ocean bottom pressure and soil moisture, respectively. Fig. 5(a) suggests correlation of higher frequency oscillations particularly for surface pressure, but longer period variations differ. Fig. 5(b) shows observed (blue) and estimated (black and magenta)  $\Delta J_2$  associated with mountain glaciers. The black line shows  $\Delta J_2$  for Alaska and Arctic glaciers, and magenta line exhibits  $\Delta J_2$  for other glaciers. Alaska and Arctic glaciers contribute some decadal and longer variations of  $\Delta J_2$  while others do not affect  $\Delta J_2$ . Fig. 5(c) includes Greenland ice mass balance ( $\Delta M_*$ ) (black). Estimated  $\Delta J_2$ from Greenland ice mass balance shows similar long-term variability to the observed  $\Delta J_2$  (blue). In particular, the recent  $\Delta J_2$  increase starting at about 2005 is largely associated with Greenland ice mass balance. Fig. 5(d) is similar to Fig. 5(c) except the black line here is for Antarctic ice mass balance. The long-term parabolic shape exhibited by the blue line is largely explained by Antarctic ice mass balance, indicating that long-term variation of earth oblateness



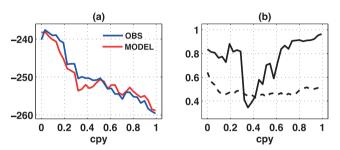
**Figure 5.** Comparison between observed (blue) and modelled  $\Delta J_2$ . For  $\Delta J_2$  calculations, geophysical models include (a) surface pressure (black, SP), ocean bottom pressure (green, OBP) and soil moisture (magenta, SM), (b) mountain glacier mass balance in Alaska and Arctic (black) and other regions (magenta), (c) ice mass balance in Greenland (black) and (d) ice mass balance in Antarctica (black).

during the last four decades is mainly associated with ice mass loss acceleration in Antarctica.

Results shown in Fig. 5 imply that Greenland and Antarctic ice mass balance is a major cause of long-term and decadal  $\Delta J_2$ variations while higher frequency variations result mostly from atmospheric pressure. Now we combine all climate components to compare with  $\Delta J_2$  observations. Fig. 6 shows observed (blue) and estimated (red)  $\Delta J_2$ , the combined effect of surface pressure, ocean bottom pressure, soil moisture, mountain glaciers and polar ice sheets. Now the two time-series agree remarkably with each other (with a correlation coefficient r = 0.86, and *p*-value is close to zero). Excellent correlation and comparable magnitudes indicate that long-term global mass redistribution estimates used here are reasonably accurate. This is particularly important because they imply a good estimate of the pre-GRACE history of ice mass balance in polar regions, potentially useful for projecting future sea level variations. Blue and red numbers in the figure represent the acceleration coefficients (2nd order polynomial coefficient) for ob-



**Figure 6.** Comparison between modelled (red) and observed (blue)  $\Delta J_2$ . Modelled  $\Delta J_2$  includes contributions from soil moisture, atmospheric and ocean bottom pressure, and mountain glacier and polar ice sheet mass balance.

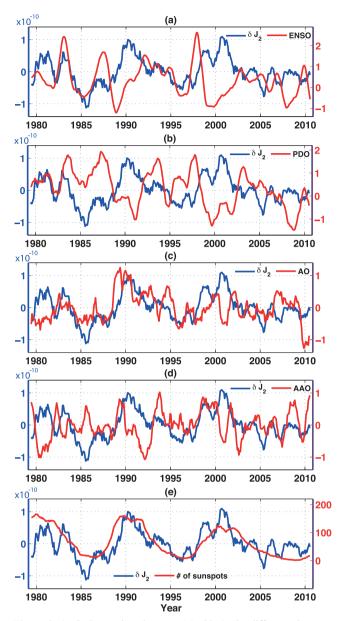


**Figure 7.** (a) Power spectra of observed (blue) and modelled (red)  $\Delta J_2$ . The vertical scale is in decibels. (b) Coherence between modelled and observed  $\Delta J_2$  (solid black) and its 95 per cent uncertainty level (dash black).

servations and model estimate, respectively. The two acceleration rates also agree with each other within the stated uncertainty, which corresponds to a 95 per cent confidence interval considering polynomial misfit with a conventional assumption of normally distributed independent residuals.

Although Fig. 6 shows good agreement between observation and model estimates, there are some differences. In particular, an abrupt  $\Delta J_2$  increase is observed in 1998 but is only partly present in the model  $\Delta J_2$ . Chao *et al.* (2003) found a similar result and suggested that ocean models do not properly simulate water mass redistribution at long periods, in particular those associated with the PDO. Similar disagreements between modelled and observed  $\Delta J_2$  are also found during 1985–1987 and 1990–1992. Overall, amplitude differences between observed and modelled  $\Delta J_2$  suggest underestimation of modelled  $\Delta J_2$  in the presence of otherwise similar temporal variability.

The correlation coefficient (r = 0.86) is a broad-band measure of correlation, but it is also possible to analyze correlation as a function of frequency using power spectra and coherence analysis. Fig. 7(a)shows the power spectra of observed and modelled  $\Delta J_2$  using a multitaper (six taper) method. Since seasonal cycles are removed and an 11-months moving average is applied, frequencies above 1 cycle per year (cpy) are not of interest. There are 32 spectrum values between 0 and 1 cpy (nominal bandwidth of 0.03 cpy), but the bandwidth of each estimate is 0.19 cpy, due to spectral smoothing associated with the 6 tapers. The two power spectra are similar to each other except around 0.35 cpy (~3 year period) where the model power spectrum falls below the observed by about 3 decibels, suggesting that the model lacks a signal important in this frequency range. Fig. 7(b) exhibits the coherence spectrum as a companion to the power spectra in Fig. 7(a). A 95 per cent confidence level for significant coherence is estimated by a Monte Carlo method (1000 trials) which takes into account the non-white nature of the power spectra, and the duration of the time-series. The solid black line in



**Figure 8.** (a–d) Comparison between  $\delta J_2$  (blue), the difference between observed and modelled  $\Delta J_2$ , and climate indices (red). (e) Similar plot to (a–d) except that the red line is the number of sunspots.

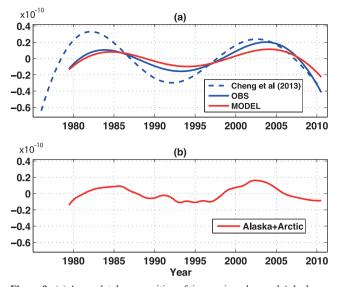
Fig. 7(b) shows the coherence, and the dashed black line represents the 95 per cent confidence level. The coherence is significant except near 0.35 cpy as indicated in Fig. 7(a). This suggests a missing component in the model time-series, and it is consistent with the appearance of observed and modelled  $\Delta J_2$  in Fig. 6 that shows some differences at interannual timescale.

Fig. 8 shows (in blue) the residual  $\delta J_2$ , the difference between observed and modelled  $\Delta J_2$  (shown in Fig. 6). We interpret  $\delta J_2$  as reflecting both limitations of climate model estimates (Chao *et al.* 2003) and possibly long-term geodetic variations of other origins (Cheng *et al.* 2013). Figs 8(a)–(d) compare  $\delta J_2$  with several climate indices (in red), including ENSO, PDO, AO and AAO, respectively. It appears that climate indices correlate with  $\delta J_2$  during particular time spans. For example, ENSO and PDO indices show opposite variations to  $\delta J_2$  during 1998–2010. In general, variations of the AO index and  $\delta J_2$  are similar to each other during 1983–1998, and those between AAO and  $\delta J_2$  are opposite during 1979–1988. The suggestion from Fig. 8 is that multiple climate oscillations may affect earth oblateness, but it is difficult to be more definite without further investigation of how well these climate oscillation signals are represented in the climate model predictions.

The residual  $\delta J_2$  also shows apparent oscillations with a period near 10-yr. Cheng & Tapley (2004) also found a similar period (~10.6-yr) in  $J_2$  based on wavelet decomposition. Solar activity (measured by the number of sunspots) varies with an 11-yr period, as shown by the red line of Fig. 8(e) after applying an 11-month moving average as done to  $\Delta J_2$ . There appears to be correlation with  $\delta J_2$  over most of 1979–2010, especially since the early 1980s. In addition,  $\delta J_2$  appears to track the recent unusual solar minimum of 2008 (Russell et al. 2010), which was delayed from the expected year of 2006. Since solar irradiance is very stable during the course of a solar cycle, it is not likely that solar activity has contaminated SLR solutions by variation of solar radiation pressure (John Ries, University of Texas at Austin, personal communication). Another suggestion that might be taken from Fig. 8(e) is that solar activity influences Earth's climate (Meehl et al. 2009), altering air or water mass redistribution in some fashion not yet incorporated in climate models. In the analysis here, we used GLDAS-2 and GECCO for land and ocean mass redistribution, respectively. These models may have limited skill in representing climate variations associated with the approximately 11-yr solar cycle.

It is also possible that decade-scale components of  $\delta J_2$  may be related to the lunar nodal tides at 18.6- and 9.3-yr periods, but while  $\delta J_2$  in Fig. 8 shows oscillations near a period of 10 yr, an 18.6-yr variation is not evident. The 9.3-yr tide is about 30 times smaller than the 18.6-yr tide (Cheng & Tapley 2004), so it would be an unlikely explanation for the ~10-yr variation seen in  $\delta J_2$ .

Earlier studies by Cheng & Tapley (2004) and Cheng et al. (2013) noted variations near the 18.6-yr period in their residual  $J_2$  timeseries. They discussed as possible causes ocean tides and anelastic mantle response for long-period ocean loading. A similar residual is not apparent in our  $\delta J_2$ , and we show here that climate contributions in our model time-series have accounted for these rather than ocean tides. We first replicate the residual time-series given by Cheng et al. (2013). Observed  $\Delta J_2$  time-series from January 1976 to May 2010 are decomposed using a level 7 'dmey' wavelet as in their study. A quadratic fit is removed from the decomposed time-series, and the result is shown in the dashed blue line of Fig. 9(a). This is identical to the dashed blue line of Fig. 2 in Cheng et al. (2013). The same wavelet decomposition is applied to observed  $\Delta J_2$  (blue line in Fig. 6) from January 1979 to December 2010, and the quadratic fit is removed from the decomposed time-series. The two wavelet decomposed time-series exhibit large amplitude difference while their phases are similar. Amplitude differences are probably due to the different lengths of time-series and data reduction before applying the wavelet decomposition. Prior to the wavelet transform, here we remove linear trends and seasonal cycles from observed and modelled  $\Delta J_2$  while Cheng *et al.* (2013) retained linear trend and seasonal terms. The solid red line shows a similar time-series to the solid blue line except that wavelet decomposition is applied to our model  $\Delta J_2$  (red line in Fig. 6). The two time-series show similar variations, about two cycles during the period 1979-2010. This confirms that the apparent 18.6-yr oscillation is not associated with ocean tides but instead is explained by climate phenomena because model  $\Delta J_2$  does not include any effect from tides. Fig. 9(b) shows that these variations are probably associated with Alaska and Arctic glaciers. The red line shows  $\Delta J_2$  contributions from Alaska and Arctic glaciers after a 2nd-order polynomial fit is removed.



**Figure 9.** (a) A wavelet decomposition of time-series: observed  $\Delta J_2$  shown in Cheng *et al.* (2013) (dashed blue), observed  $\Delta J_2$  used in this study (solid blue) and modelled  $\Delta J_2$  (solid red). (b)  $\Delta J_2$  from mountain glacier mass balance in Alaska and Arctic. Quadratic terms are removed.

About two cycles of an oscillation are apparent from 1979 to 2010, with phase and amplitude similar to the solid red line in Fig. 9(a). The conclusion is that an ocean tidal source for the apparent 18.6-yr variation in  $\Delta J_2$  is unlikely, but decadal variations of glacier mass balance are a likely cause of the apparent long-period oscillation in  $\Delta J_2$ .

## **4** CONCLUSIONS

Predictions of Earth dynamic oblateness changes  $(\Delta J_2)$  from geophysical models (atmosphere, hydrosphere and cryosphere) agree reasonably well with  $\Delta J_2$  variations observed by SLR. Nerem & Wahr (2011) found that polar ice mass balance was an important contributor to long-term change of  $\Delta J_2$  during the GRACE era. Cheng et al. (2013) examined  $\Delta J_2$  variation before the GRACE era but the results were limited in accounting for  $\Delta J_2$  without estimates of interannual and longer ice mass changes in Greenland and Antarctica over most of the SLR observation period. By combining model estimates and observations, we can reconstruct previous polar ice mass balance from 1979 to 2010, and it now is clear that Greenland and Antarctic ice mass variations are the main driving forces of long-term  $\Delta J_2$  variations during the last four decades. This is potentially important because polar ice mass variations were poorly understood before the GRACE era. An extended multidecadal polar ice mass variation estimate should be useful for sea level forecasts.

It has been suggested that  $\Delta J_2$  would include effects of the 18.6 yr tide (Cheng & Tapley 2004). While a variation near this period is present in the observed time-series, Alaska and Arctic glacier mass change mostly account for it. Residual  $\delta J_2$  variations show a clear oscillation near 10–11 yr. Correlations with the sunspot time-series are intriguing, suggesting some connection with solar activity. This connection might be through climate-related variations of mass redistribution which alter Earth's  $J_2$ , or other unknown causes. Further investigation is needed to better understand the cause of the 10–11 yr residual  $\delta J_2$  variations and connections with the solar cycle.

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